

· Jota structure for maintaining cc's







onnected components

Say $S \sim f$ if connected in undirected graph Then \sim is equivalence relation

- · reflexive
- Symmetric
- transitive

Partition into convected components (CCS)

Nexchable from S

Puntime of
$$BFS: -every edge used
 $\leq 2x$.
 $-2M_{C_S}$ fotal vertices
 $O(M_{C_S})$
 $-M_{C_S}= \# edges in$
Using Queue $C_S: cc of s$.$$

(C algo:



Memoized

- If P(v) = Folse: D(v) = D(u) + 1
- For (U,V) EE: S. Rush (U,V) include parent into
- Unversionable SSSP Let p(v) be the parent of v: $V \ge 00000$ for the first time due to the edge (p(v),v) $(l \ge 0 (S, V) = 1 + d(S, p(v)))$ With $(l \ge 0, Simple modes (amplie SSSP!)$

Proof of claim: (If
$$R_0 = \langle S \rangle$$

 $P_1 = \langle \partial(S_1 \cdot) = 1 \rangle$
 $R_2 = \langle \partial(S_1 \cdot) = 2 \rangle$
;

(Laim is that they form "frontiers" in S:



Base case: Ro V

let
$$V \in R_i$$
 be dequeued
All (v, u) have $\partial(S, u) \leq i + 1$
 $\{f \mid \partial(S, u) \leq i$ then reached (induction). \checkmark

-XJMgUL





Preorder: Stuvw Postorder: Vwuts

Key (12:m! If input is DAG, then postorder reversed = topological order!



T: V. finish $\leq W.$ finish

(Z) same

